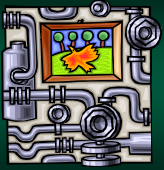


# Stacks & Queues

Part 3

1



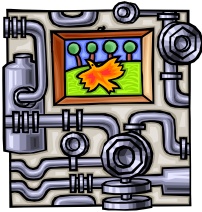
# Data Abstraction

Abstraction is power

2

## Abstract Data Types

- *Data types* are used in practically all programming languages
- The core data types found in language is known as a *primitive data type*

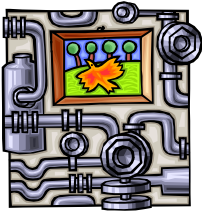


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## Data Types Specify 2 Things

1. Set of possible values
2. *Operations* on the data
  - these are alternatively called *functions* or *methods*
  - data types often define the errors can occur during each operation



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## Integer Example

- *int* is a type (found in most languages)
- The 32-bit version can contain values from  $-2^{31}$  to  $2^{31} - 1$

```
int n;
```

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## Integer Example

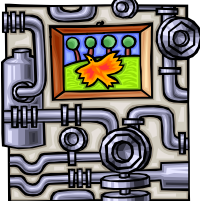
- Operations include:  $+$ ,  $*$ ,  $-$ ,  $/$ ,  $\%$ , and many more (e.g. comparisons)

```
int n;
```

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## Abstract Data Types

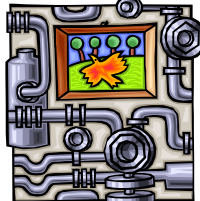


- An *abstract data type (ADT)* hides how it is implemented from the *client* (programmer)
- The client only interacts with the defined operations

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## Abstract Data Types

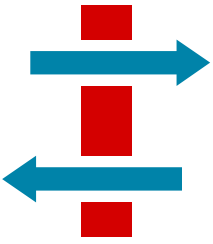


- This layer of abstraction separates implementation from behavior
- And, it allows you to change the data structure – without breaking the ADT

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## ADTs vs Data Structures

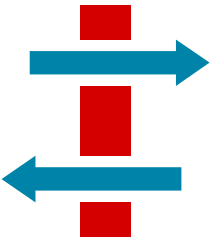


- An ADT is implementation independent
- Can, internally, use any data structure
  - array, linked list, etc...
  - depending how the ADT works, some are better than others

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## ADTs vs Data Structures

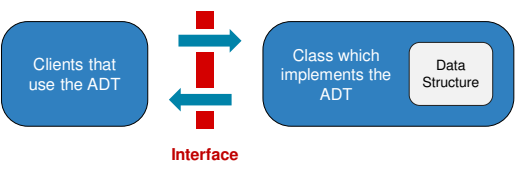


- ADT defines an *interface*
- It defines:
  - operations (public methods)
  - properties (public fields)

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## Data Structures

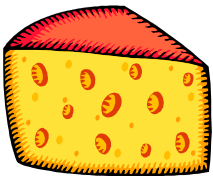


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## Example ADT: Cheese Trader

- Data stores orders of cheese
- The operations supported are
  - buy (cheese, count)
  - sell (cheese, count)
  - cancel (Order)
  - balance – current funds

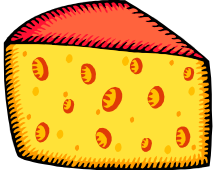


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## Example ADT: Cheese Trader


- Error conditions:
  - nonexistent cheese
  - sell a cheese we don't have
  - count is not greater than 0



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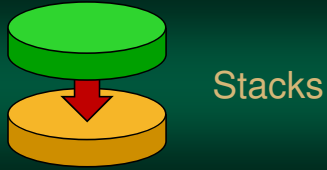
## Cheese Trader Interface



```
public class CheeseTrader
{
    int buy(String name, int count) Returns order #
    int sell(String name, int count) Returns order #
    void cancel(int order)
    double balance()
}
```

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Stacks

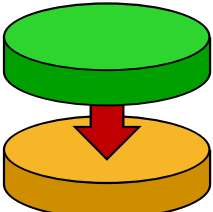
Piles of... Data

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## Stack

- The *Stack ADT* stores objects based on the concept of a stack of items – like a stack of dishes
- Data can only be added to or removed from the top of the stack

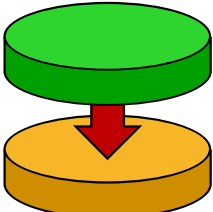


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## Stack

- This gives a **first-in-last-out** logic (aka FILO)
- Same concept is also called **last-in-first-out** (LIFO)

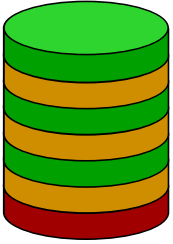


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## Stack Operation: Push

- A value is added to the stack
- It is placed on the top location
- Rest of the items are "covered"



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## Push Location

- Pushed items are added at the front of a list
- So, any pushed item is placed at the head



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## Push Location

- Pushed items are added at the front of a list
- So, any pushed item is placed at the head



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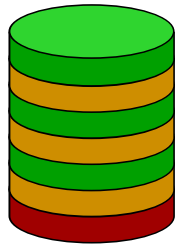
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## Stack Operation: Pop

- Removes an item from the stack
- Last item added is removed
- 2<sup>nd</sup> item becomes the top



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## Pop Location

- Popped items are removed from the front of a list
- So, any popped item is taken from the head



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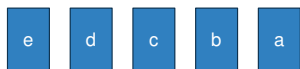
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## Pop Location

- Popped items are removed from the front of a list
- So, any popped item is taken from the head



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## Stack Interface

```
public class Stack
{
    Stack () Create empty stack
    void push(Object item)
    Object pop ()
    Object top () Return top. Sometimes called Peek()
    bool isEmpty ()
}
```

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## Stacks: Error Conditions

- The execution of an operation may sometimes cause an error condition, called an *exception*
- Exceptions are said to be “thrown” by an operation that cannot be executed
- In the Stack ADT, operations pop and top cannot be performed if the stack is empty

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## Resizing an Array-Based Stack

- For stacks, if a dynamically allocated array is used, each pop/push will require the entire array to be resized
- It will require  $O(n)$
- So, a dynamic array is a poor choice



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## One Solution... Not a Great One

- The array *could* grow/shrink by a specific # of elements
- So, the array will resize only when a new “block” of elements is needed
- Like a fixed-capacity array, we need to keep an end index



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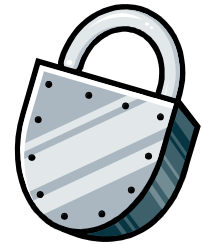
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## Fixed-Capacity Stacks

- A fixed-capacity array can be used instead
- For a *fixed-capacity stack*, an array is an excellent choice – in specific situations...



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## Array-Based Fixed-Capacity Stack

- The stack would behave as normal until the capacity is reached
- In this case, one of two things will happen...



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## When the Stack is filled...

1. Stack throws an *Overflow Error*
2. Stack discards an object
  - the bottom of the stack is typically removed
  - this gives the space needed for the newly pushed object
  - e.g. the history feature of your web browser

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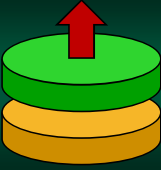
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### Stack Summary

Operation	Fixed-Capacity Array	Resizable Array	Linked List
Pop()	O(1)	O(n)	O(1)
Push()	O(1)	O(n)	O(1)
Top()	O(1)	O(1)	O(1)

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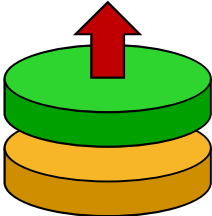
## Queues

Conga-line of Data!

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### Queues

- *Queue ADT* stores list of arbitrary objects
- Based on the concept of a line – e.g. when you buy groceries
- Objects enter the back of the line, and must wait for prior items to leave before they do

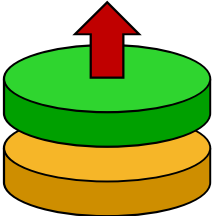


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### Queues

- In most parts of the World, they call a "line" a "queue"
- Main queue operations:
  - **enqueue** (object): place on item on the queue
  - **dequeue**: removes and returns the first inserted object

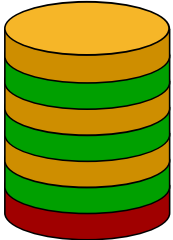


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### Queue Operation: Enqueue

- When an object is "enqueued", it is put on to the **end** of the queue
- The items on the top of the queue are not covered




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### Enqueued Location

- Enqueued items are added at the end of a list
- So, any enqueued item is placed at the tail



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## Enqueued Location

- Enqueued items are added at the end of a list
- So, any enqueued item is placed at the tail

a

b

c

d

e

f

g

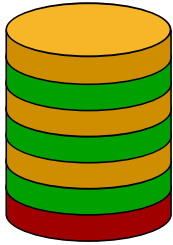
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## Queue Operation: Dequeue

- Dequeue removes the item from the front of the queue
- Second item becomes the new first item
- This gives a first-in-first-out logic (aka FIFO)



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## Dequeued Location

- Dequeued items are removed from the front of a list
- So, any dequeued item is taken from the head

a

b

c

d

e

f

g

h

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## Dequeued Location

- Dequeued items are removed from the front of a list
- So, any dequeued item is taken from the head

d

e

f

g

h

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## Auxiliary Queue Operations

- Queues also tend to have some operations defined
- These are not necessary, but they are useful
- Auxiliary operations:
  - **peek**: return the next object without removing it. This is also sometimes called "front"
  - **size**: returns the number of objects on the queue
  - **isEmpty**: indicates whether the queue contains no objects. This is an alternative to size()

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## Queue Interface



```

public class Queue
{
    Queue () Create empty queue
    void enqueue (Object item)
    Object dequeue ()
    int size ()
    Object peek () Return first item, without dequeue
}
    
```

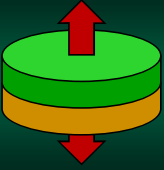
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### Queue Summary

Operation	Fixed-Capacity Array	Resizable Array	Linked List
Enqueue()	$O(1)$	$O(n)$	$O(1)$
Dequeue()	$O(1)$	$O(n)$	$O(1)$
Peek()	$O(1)$	$O(1)$	$O(1)$

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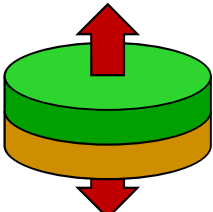
### The Deque ADT

Time to shuffle the "deck"

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### Deque ADT

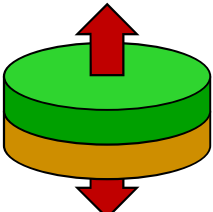
- There is a variant of the queue called a *deque* (pronounced "deck")
- The name is derived from **d**ouble-**e**nded **q**ueue (sometimes it is shorted more to DQ)



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### Deque ADT

- As the name implies, it's a queue allows insertions and removals from both ends
- It is a merging of a stack and queue ADT and the operations are union of the two
- Be warned:** name of each operation varies **greatly** between programming languages



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### Deque ADT

- addFront**
  - place an object on the front of the deque
  - this is same as stack "push"
  - also called: offerFirst, pushFirst
- addBack**
  - place an object on the end of the deque
  - this is the same as queue "enqueue"
  - also called: offerLast, pushLast

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### Deque ADT

- removeFront**
  - remove an object from the front of the deque
  - same as: queue "dequeue" or stack "pop"
  - also called: pollFirst, popFront
- removeBack**
  - this is unique** – and not found in either a stack or queue ADT
  - also called pollLast, popBack

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## Deque Interface

```
public class Deque
{
    Deque() Create empty deque
    void addFront(Object item)
    void addBack(Object item)
    Object removeFront()
    Object removeBack()
    Object peekFront()
    Object peekBack()
    bool isEmpty()
}
```

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## Deque Example

1. addFront('N') 
2. addBack('E') 
3. addFront('W') 
4. addBack('D') 
5. addFront('P') 

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## Deque Example

1. addFront('N')
2. addBack('E')
3. addFront('W')
4. addBack('D')
5. addFront('P')



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## Deque Advantages

- A deque can function as either a stack or queue
- "Add Front" operation can be used to "redo" or "undo" a queue removal – remove then put it back in line
- There are some scenarios where this logic is needed

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## Deque Disadvantages

- While, Stacks/Queues can be created with a single-linked-list, *a Deque requires a double-linked-list*
- ...otherwise, removing items from the end would require  $O(n)$  – *even with a tail node*
- Also, the link overhead (memory requirements) is doubled

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## Deque Summary

Operation	Fixed Array	Resizable Array	Single Linked List	Double Linked List
addFront()	$O(1)$	$O(n)$	$O(1)$	$O(1)$
addBack()	$O(1)$	$O(n)$	$O(1)$	$O(1)$
removeFront()	$O(1)$	$O(n)$	$O(1)$	$O(1)$
removeBack()	$O(1)$	$O(n)$	$O(n)$	$O(1)$

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## Queues & Stacks in Practice

1001 Uses!  
(I meant 1,001 – not 9)

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## HTML Tag Matching

- HTML is a hierarchical structure
- HTML consists of tags
  - each tag can also embed other tags
  - allows text to be aligned, made bold, etc...



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## HTML Tag Matching

- Web browsers read the text and apply a tag depending if it is active
- They maintain a stack...
  - push a start tag, pop and end tag
  - if the HTML is correct, they should match
  - ... with the exception of the unary tags

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## HTML Tag Matching

```

<html>
<body>
<center>
<h1>Banks of Sacramento</h1>
</center>
<i>A bully ship and a bully crew.<br>
Hoo-da! Hoo-da!<br>
A bully mate and a captain too.<br>
Hoo-da! Hoo-da-day!<br>
And it's blow, ye winds, blow,<br>
for Californi-o.<br>
For there's plenty of gold,<br>
so I've been told,<br>
on the banks of the Sacramento.</i>
</body>
</html>

```

**Banks of Sacramento**


*A bully ship and a bully crew.  
Hoo-da! Hoo-da!  
A bully mate and a captain too.  
Hoo-da! Hoo-da-day!*

*Then blow, ye winds, blow,  
for Californi-o.  
For there's plenty of gold,  
so I've been told,  
on the banks of the Sacramento.*

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## Balanced Parentheses

- When analyzing arithmetic expressions often the structure of the expression needs to be checked
- For example:
  - are operators in the correct place?
  - are the parenthesis balanced?



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## Balanced Parentheses

- Let's look at parenthesis
- One approach...
  - can we just use a "parenthesis count"
  - if it isn't 0 at the end then the expression is invalid
- Sorry, it won't work...
  - some expressions allow { } and [ ]
  - ...and they may be in the wrong place

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## Balanced Parentheses

- A great solution is a stack
- Approach...
  - push each ( and pop each )
  - at the end, the stack should be empty
  - also, if you attempt to pop on an empty stack, the expression is invalid
- It can also catch mismatched symbols

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## Balanced Parenthesis Examples


( a + b )	Balanced
( a + b ) )	Pop empty stack
) a + b (	Pop empty stack
( a + ( b + 1 ) * c ) / e	Balanced
( a * ( b + ( ( d + e ) * f ) )	Stack has 1 left

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## Balanced Parenthesis Examples

[ a + b ]	Balanced
( a + b )	Mismatch
{ [ a + b ] }	Mismatch
( a + ( b + 1 ) * c / e	Unbalanced
( a * [ b + { c + d } * e ] )	Balanced

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## Evaluating Expressions

A Stack and Queue working together!

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## Evaluating Expressions


- It is a common task in programs to **evaluate** mathematical expressions and get a result
- Computers can perform this task using an algorithm *created by Dijkstra*, but we will get into that later



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## Evaluating Expressions

- First, we need to look at mathematical expressions
- We usually use **infix** notation
  - not stack or queue "friendly"
  - there are, however, two alternative notations
  - one of which is stack friendly*



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## Infix Notation

- Using *infix notation*, we put the operator in between the two operands
- This is the standard format used today

To add the numbers  $a$  and  $b$ , we type:  $a + b$

To divide  $a$  by  $b$ , we type:  $a / b$

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## Prefix Notation

- Prefix notation*, rather than putting the operator between the operands, puts it first
- It is also called "*Polish Notation*"
- Used by the LISP programming language

To add the numbers  $a$  and  $b$ , we type:  $+ a b$

To divide  $a$  by  $b$ , we type:  $/ a b$

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## Postfix Notation

- Postfix notation* puts the operator at the end
- Also called "*Reverse Polish Notation*" (*RPN*)
- Since the operator is last, we can also use it as a "trigger" to perform math

To add the numbers  $a$  and  $b$ , we type:  $a b +$

To divide  $a$  by  $b$ , we type:  $a b /$

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## Where are My Parenthesis?

Infix	Prefix	Postfix
$a + b * c$	$+ a * b c$	$a b c * +$
$(a - b) * c$	$- a b * c$	$a b - c *$
$(a / (b - c) + d)$	$+ / a - b c d$	$a b c - / d +$
$(a + b / (c - d))$	$+ a / b - c d$	$a b c d - / +$

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## Where are My Parenthesis?

- Infix is the only notation that needs parentheses to change precedence
- The order of operators handles precedence in prefix and postfix



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## Compute Postfix Algorithm

- Computing a postfix expression is easy
- All you need is:
  - one queue that contains the values & operators
  - and one stack
- In fact, on classic Hewlett Packard calculators, all operations are stack based



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### Compute Postfix Pseudo-code

```

while there is data in the input queue
  dequeue a token (value or operator)
  if it's a value, push it on the stack
  if it's an operator
    pop two numbers from the stack
    compute the result (using the operator)
    push the result on the stack
  end if
end while
...Afterwards, the final result is on the stack

```

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### Compute Postfix Demo

Input Queue: 24 10 7 - / 34 +

Stack:  $24 / (10 - 7) + 34$

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### Compute Postfix Demo

Input Queue: 10 7 - / 34 +

Stack: 24

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### Compute Postfix Demo

Input Queue: 7 - / 34 +

Stack: 24 10

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### Compute Postfix Demo

Input Queue: - / 34 +

Stack: 24 10 7

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### Compute Postfix Demo

Input Queue: / 34 +

Stack: 24 10 7

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### Compute Postfix Demo

Input Queue: / 34 +

Stack: 24 3

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### Compute Postfix Demo

Input Queue: 34 +

24 / 3

Stack:

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### Compute Postfix Demo

Input Queue: 34 +

Stack: 8

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### Compute Postfix Demo

Input Queue: +

Stack: 8 34

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### Compute Postfix Demo

Input Queue:

8 + 34

Stack:

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### Compute Postfix Demo

Input Queue:

Stack: 42

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## Converting to Prefix or Postfix

- Why are learning this... *be patient!*
- Converting infix to either postfix or prefix notation is easy to do by hand
- Did you notice that the operands did not change order? They were always *a, b, c...*
- We just need to rearrange the operators

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## Convert Infix to Prefix / Postfix

1. Make it a *Fully Parenthesized Expression (FPE)* - one pair of parentheses enclosing each operator and its operands
2. Move the operators to the start (prefix) or end (postfix) of each sub-expression
3. Finally, remove all the parenthesis

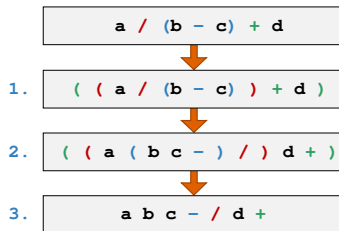
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## Infix to Postfix

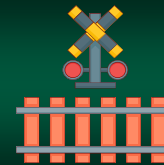


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## Infix to Postfix Algorithm

Let the computer do the work...

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## Edsger Dijkstra

- *Edsger Dijkstra* is a World-famous computer scientist
- He invented a wealth of algorithms
- For his contributions, he received the Turing Award



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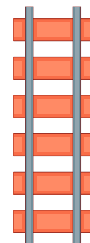
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## Infix to Postfix Algorithm

- Infix expressions need to be converted to postfix to be evaluated
- *Dijkstra's Shunting-yard algorithm* performs this task



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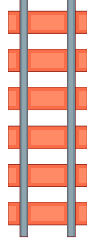
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## Shunting-yard algorithm

- Named after railroad shunting yards – which move trains onto different tracks
- Dijkstra's solution uses an input queue, operator stack, and output queue



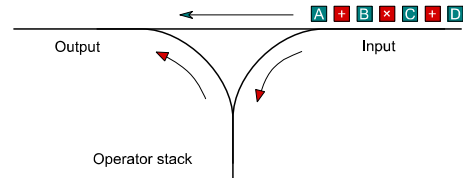
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## Shunting-yard Algorithm



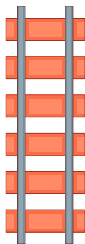
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## Shunting-yard Algorithm



- The most basic version of this algorithm requires *Fully-Parenthesized Expression*
- This means, there is no precedence and parenthesis are put around every operator

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## FPE Shunting-yard Algorithm

```

while the input queue has tokens
  read a token from the input queue
  if the token is a...
    operand : add it to output queue
    operator : push it on the stack
    '(' : push it onto the stack
  ')' :
    while the top of stack isn't a '('
      pop an operator
      add it to the output queue
    end while
    pop and discard the extra '('
  end if
end while
    
```

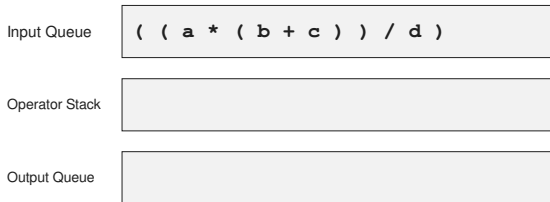
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## FPE Shunting-yard Algorithm



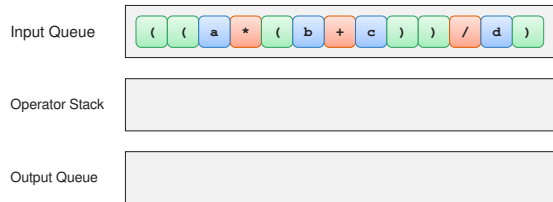
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## FPE Shunting-yard Algorithm



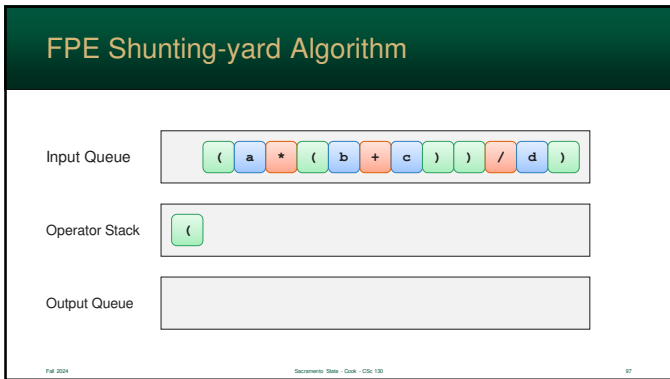
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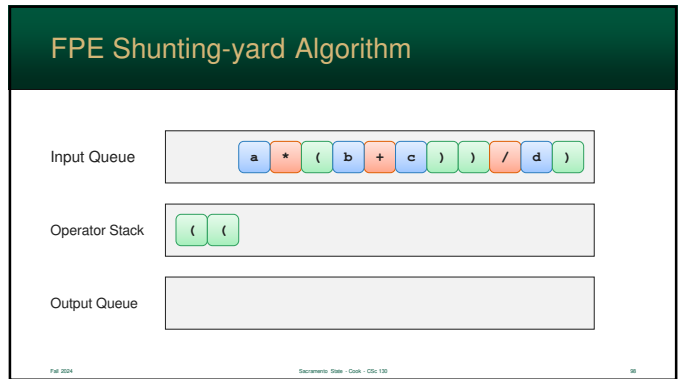
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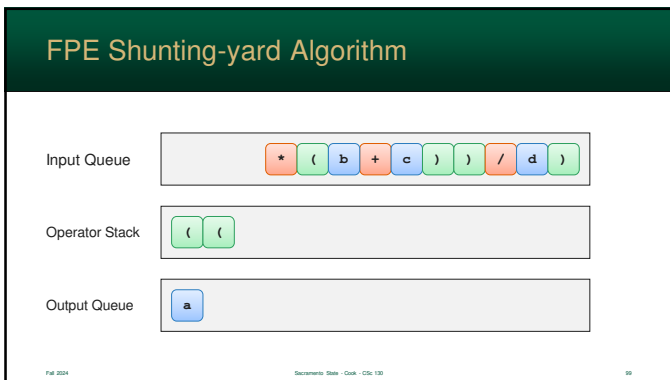




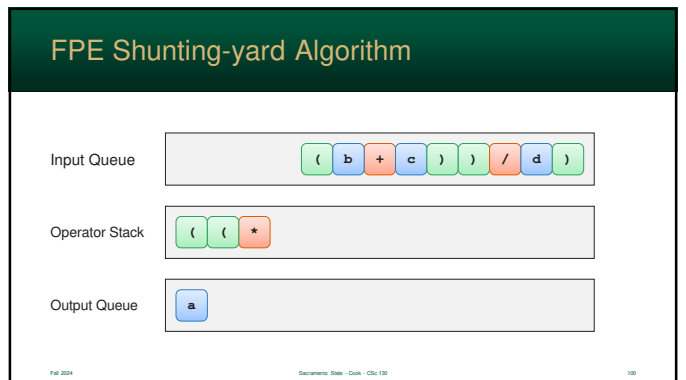
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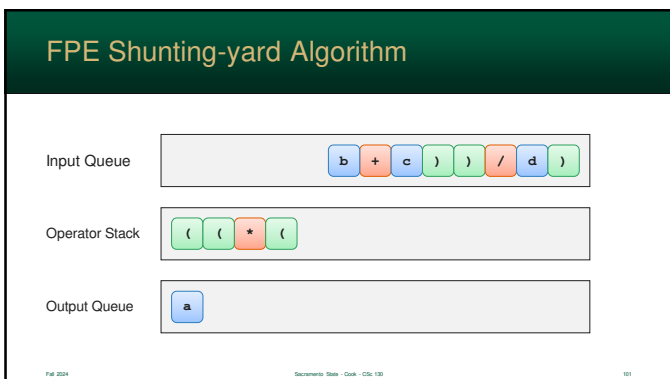
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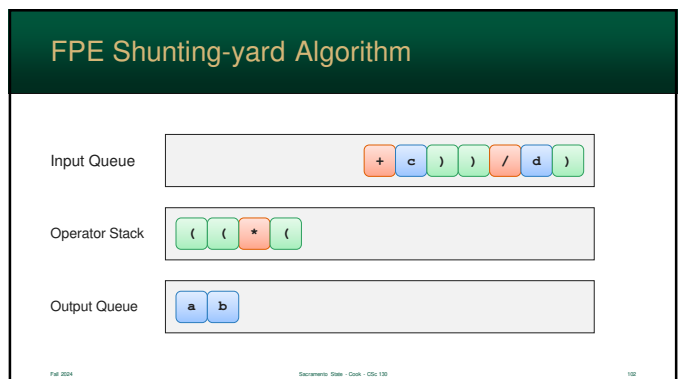
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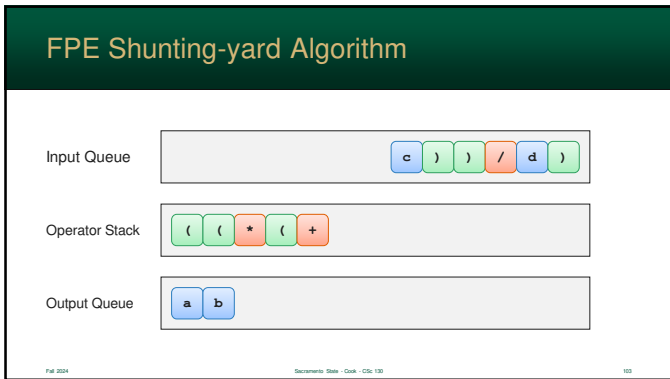
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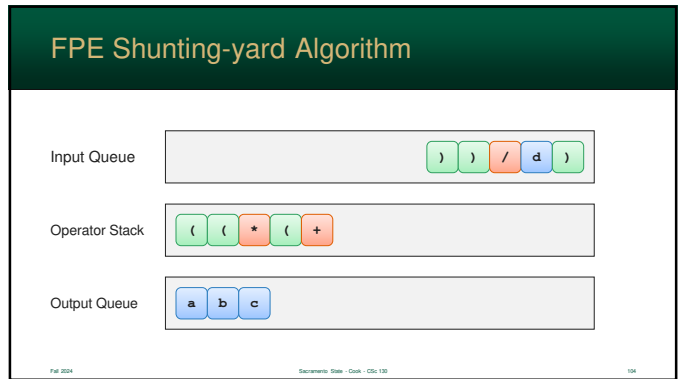
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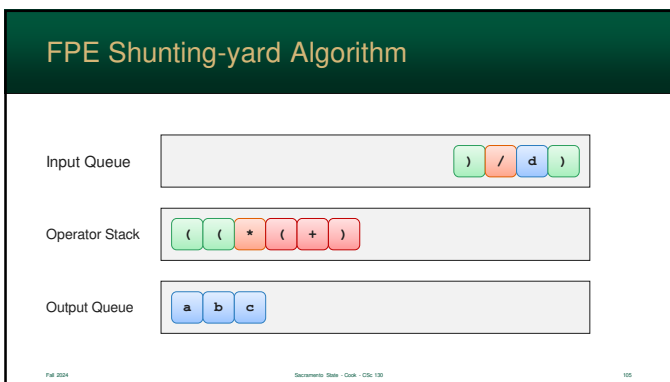
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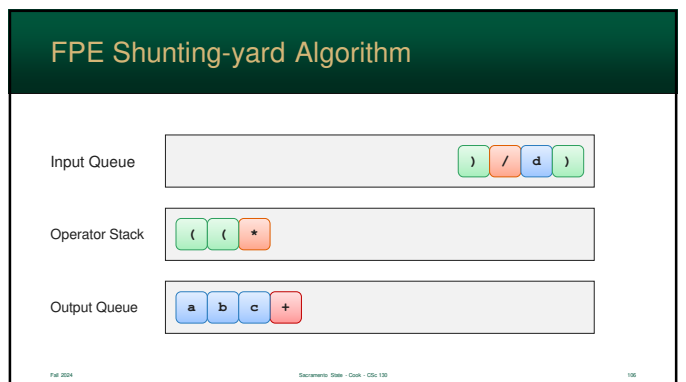
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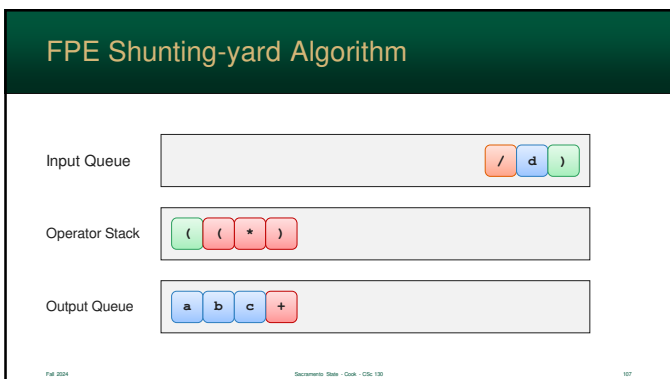
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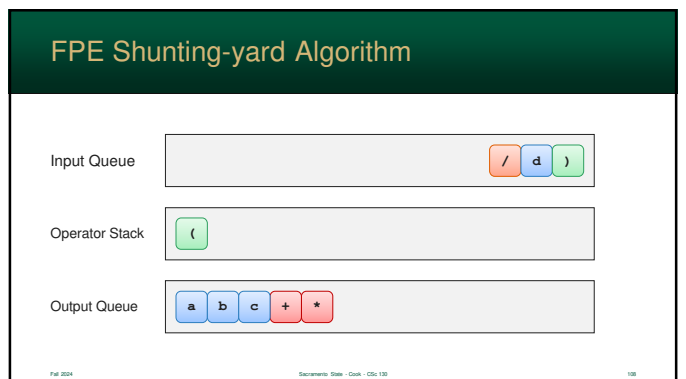
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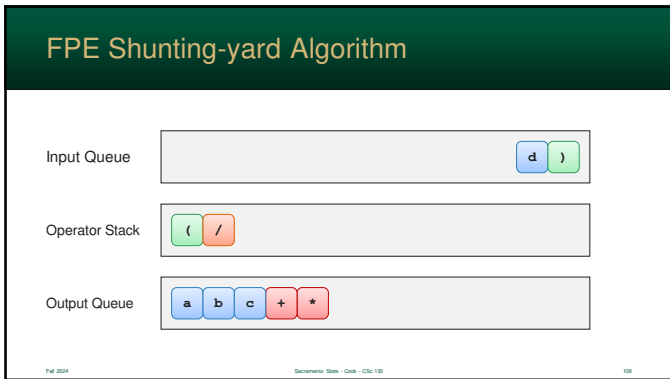
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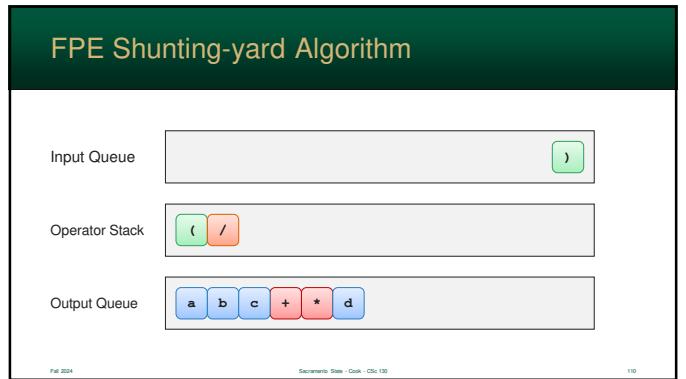
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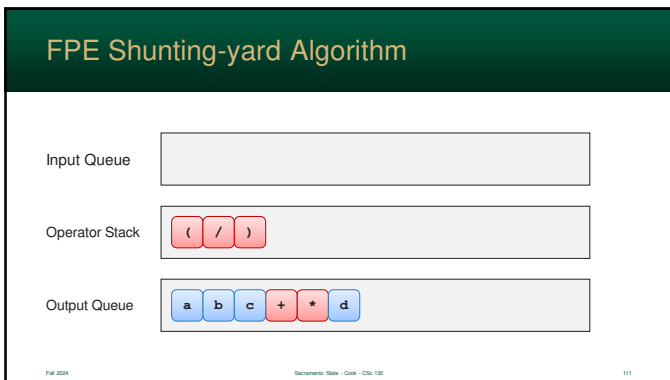
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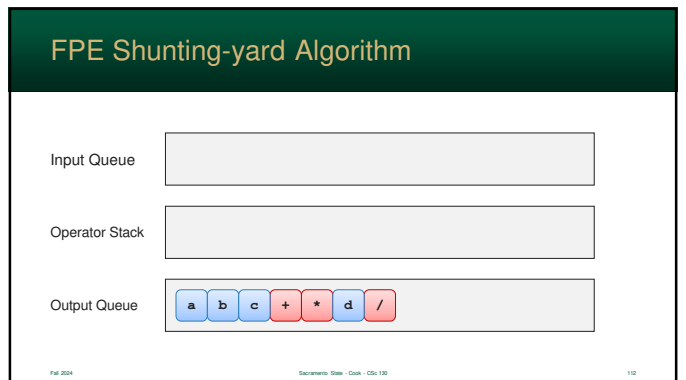
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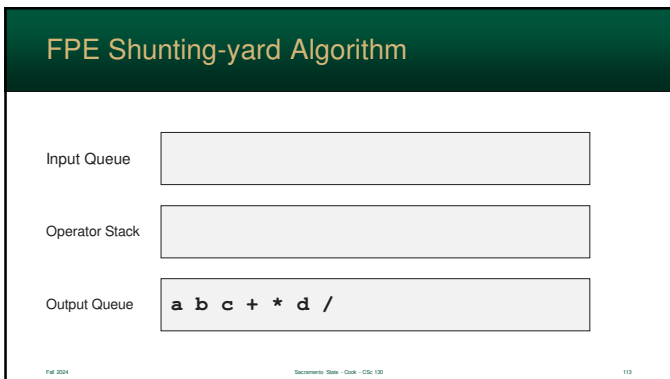
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### Too Many Paranthesis!



- FPE's are *rarely* used in real-World examples
- In fact, we use precedence rules to simplify expressions
- Fortunately, the algorithm can be modified, *very easily*, to handle precedence!

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## Non-FPE Shunting-yard Algorithm

```

while the input queue has tokens
  read a token from the input queue
  if the token is a_
    operand : add it to output queue
    operator : new rules - see next slide
    '(' : push it onto the stack
    ')' :
      while the top of stack isn't a '('
        pop an operator
        add it to the output queue
      end while
      pop and discard the '('
    end if
  end while
end while

```

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## Operator: New Rules

```

if operator is left-associative
  while top of stack is ≥ operator and not a '('
    pop the stack
    add it to the output queue
  end while
if operator is right-associative
  while top of stack is > operator and not a '('
    pop the stack
    add it to the output queue
  end while
push the operator onto the stack

```

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## Operator Associativity

Operator	Associativity
+ - * /	Left
^ (exponent)	Right

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## Shunting-yard Algorithm Example 1



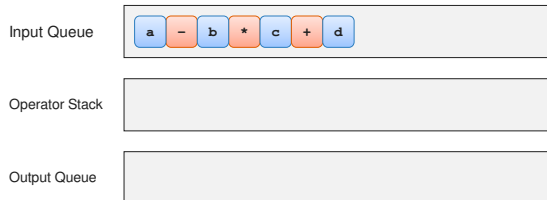
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## Shunting-yard Algorithm Example 1



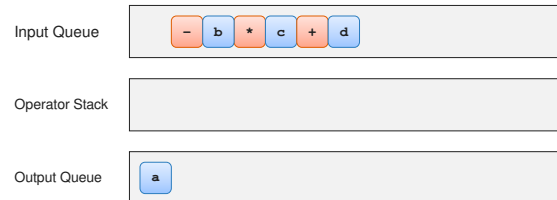
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## Shunting-yard Algorithm Example 1

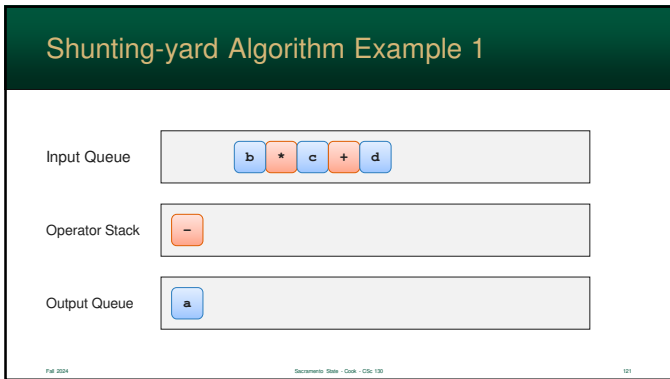


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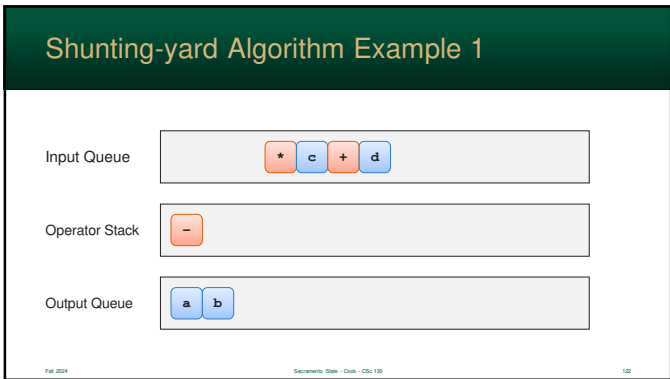
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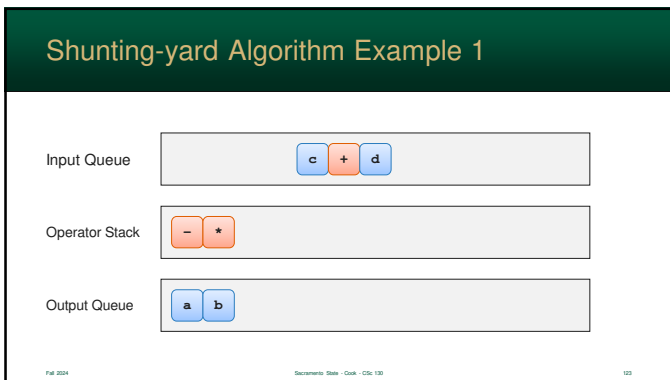
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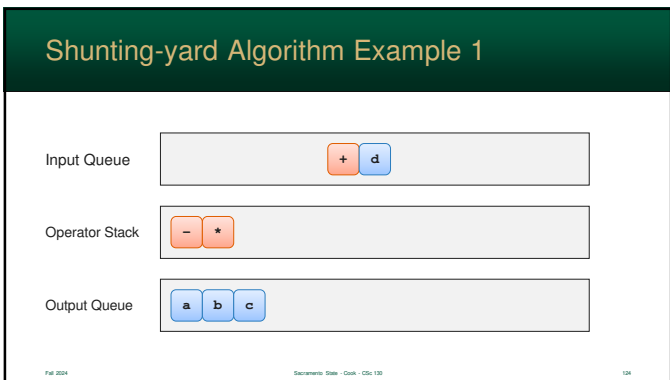
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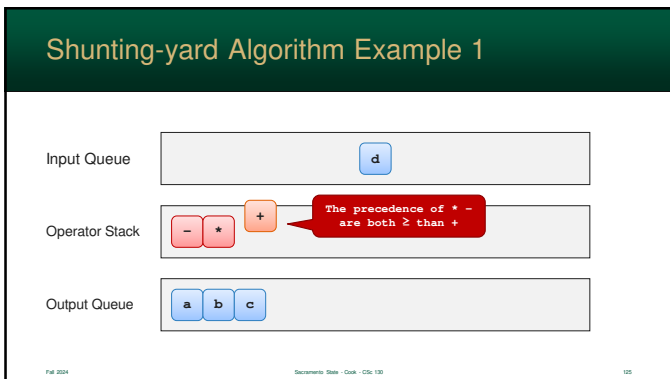
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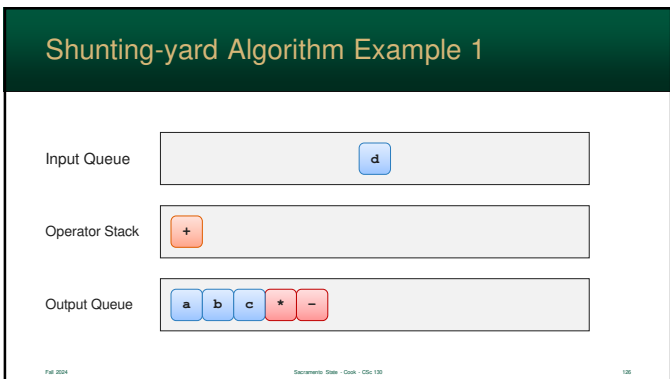
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### Shunting-yard Algorithm Example 1

Input Queue:

Operator Stack: +

Output Queue: a b c \* - d

Remaining stack items pop'd

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### Shunting-yard Algorithm Example 1

Input Queue:

Operator Stack:

Output Queue: a b c \* - d +

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### Shunting-yard Algorithm Example 1

Input Queue:

Operator Stack:

Output Queue: a b c \* - d +

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### Shunting-yard Algorithm Example 2

Input Queue: a + ( b - c \* d ) / e - f

Operator Stack:

Output Queue:

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### Shunting-yard Algorithm Example 2

Input Queue: a + ( b - c \* d ) / e - f

Operator Stack:

Output Queue:

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### Shunting-yard Algorithm Example 2

Input Queue: + ( b - c \* d ) / e - f

Operator Stack:

Output Queue: a

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### Shunting-yard Algorithm Example 2

Input Queue: ( b - c \* d ) / e - f

Operator Stack: +

Output Queue: a

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### Shunting-yard Algorithm Example 2

Input Queue: b - c \* d ) / e - f

Operator Stack: + (

Output Queue: a

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### Shunting-yard Algorithm Example 2

Input Queue: - c \* d ) / e - f

Operator Stack: + (

Output Queue: a b

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### Shunting-yard Algorithm Example 2

Input Queue: c \* d ) / e - f

Operator Stack: + ( -

Output Queue: a b

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### Shunting-yard Algorithm Example 2

Input Queue: \* d ) / e - f

Operator Stack: + ( -

Output Queue: a b c

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### Shunting-yard Algorithm Example 2

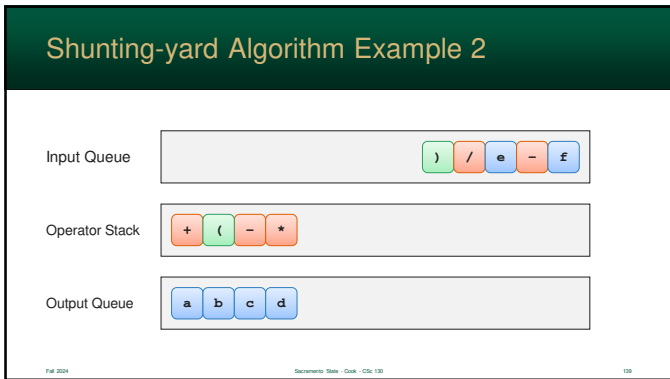
Input Queue: d ) / e - f

Operator Stack: + ( - \*

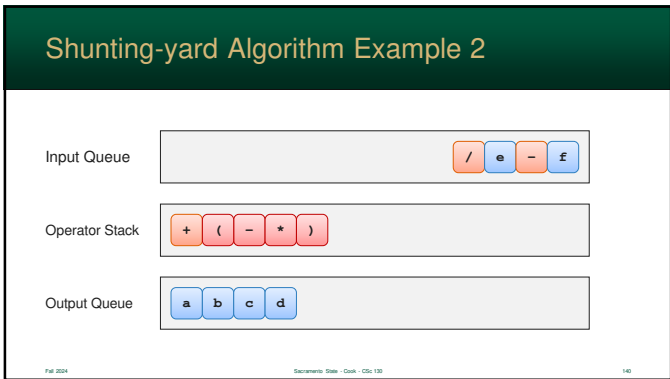
Output Queue: a b c

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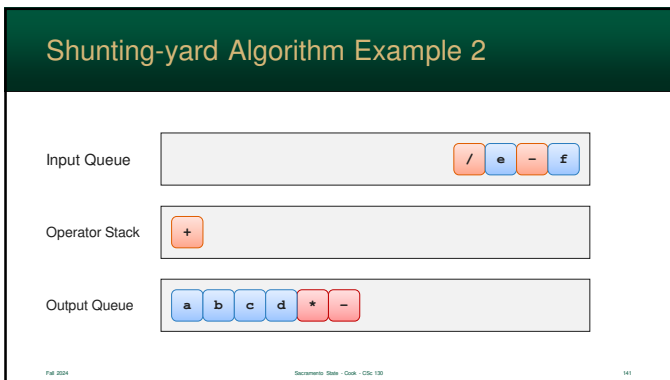
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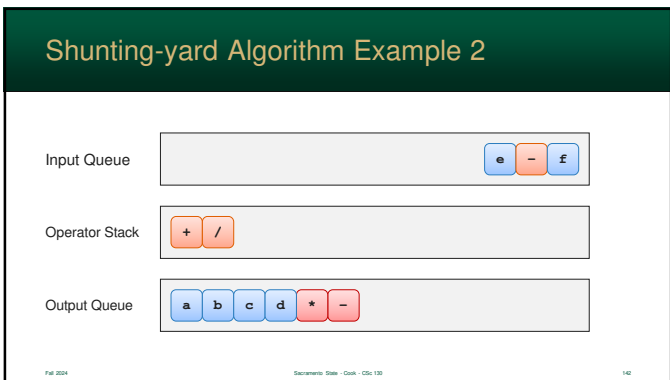
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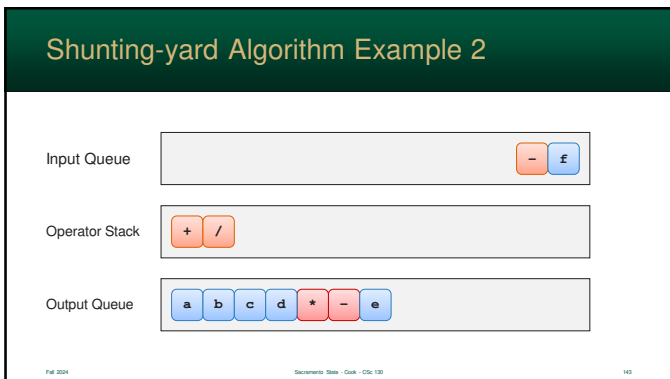
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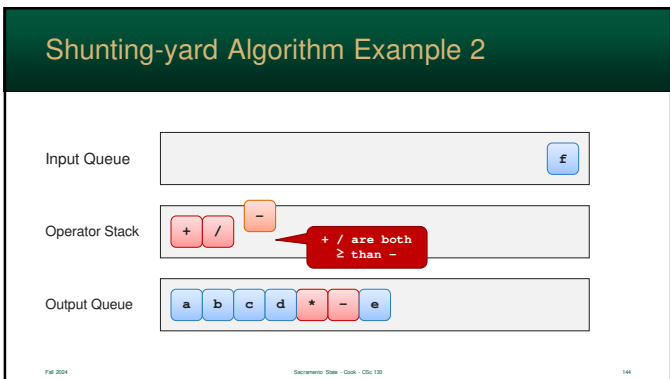
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### Shunting-yard Algorithm Example 2

Input Queue:   f

Operator Stack: -

Output Queue: a b c d \* - e / +

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### Shunting-yard Algorithm Example 2

Input Queue:  

Operator Stack: - Remaining stack items pop'd

Output Queue: a b c d \* - e / + f

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### Shunting-yard Algorithm Example 2

Input Queue:  

Operator Stack:  

Output Queue: a b c d \* - e / + f -

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### Shunting-yard Algorithm Example 2

Input Queue:  

Operator Stack:  

Output Queue: a b c d \* - e / + f -

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### Testing Our Result

$a + (b - c * d) / e - f$

↓

1. (( a + ( ( b - ( c \* d ) ) / e ) ) - f )

↓

2. (( ( a ( ( b ( c d \* ) - ) e / ) + ) f - )

↓

3. a b c d \* - e / + f -

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