







- Collections of objects indexed by other objects are called dictionaries
- They have a few alternative names...
  - keyed tables
  - symbol tables
  - maps

Dictionary Terminology

- The objects that are used for indices are called keys
- The objects that are accessed using the key are called values



### **Implementing Dictionaries**

- There are numerous approaches to implementing dictionaries
- Key-value structure
  - · a class stores a key object and value object
  - this can be stored in any data structure we have covered



### **Implementing Dictionaries** Using a linked list adding takes O(1) • access is O(n) Unsorted array • add is O(n) - have to resize • access is O(n) Sorted array add is O(n) – have to resize • access is O(log n)

8

### This Ain't So Good

- So, adding in to an array is O(n)
- Arrays seem like a poor approach
- Is there a better way to store dictionary data? Keeping adding close to O(1)?
- ... and keep access at O(log n)
- Perhaps, we will learn that soon....

### 9

7

### Databases vs. Dictionaries

- Dictionaries...
- · have a single key
- · that key is the only way to access data
- · key returns a single value
- Databases...
  - may have multiple keys (e.g. SSN, name, age, etc...)

  - · may return multiple values

10





### **Bucket Sort**

- The most basic algorithm creates a "bucket" for each of the different key values
- This "bucket" often takes the form of a queue or list



Each item in the array is • placed into the buckets based on their key

13



15









16

## **Bucket Sort**

- Then, each bucket is emptied, in order, back into the array
- This sorts the items, but algorithm has considerable storage requirements - often making it impactable













Bucket Sort: Buckets Filled	
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26



Bucket Sort: Emptied Into Array

27

### Other Bucket Sort Variations

- Proxmap Sort
  - · almost identical to the basic Bucket Sort
  - items are sorted immediately when placed in the bucket usually an Insertion Sort
- Histogram Sort (aka Counting Sort)
  - does an initial scan of the array and creates buckets the exact size that they will be filled
  - · greatly minimalizes overhead

# Other Bucket Sort Variations

- Postman's Sort
  - · very similar to the next sort we cover: Radix
  - sorts items by "category" of the key
- Shuffle Sort
  - array is recursively sub-divided, sorted, and merged/concatenated when complete
  - 2-bucket Shuffle Sort is essentially a Quick Sort with the pivot acting as divider between the two buckets

Bucket Sort		
îme Average	$O(n + (n^2 / b) + b)$ where b is the # of buckets	
ime Best	$O(n)$ when $b \approx n$	
Fime Worst	O(n <sup>2</sup> ) if Insertion Sort is used	
Auxiliary space	O(b + n)	
table	Yes	
nline?	Yes (bucket filling stage only)	

31



Computer Science to the rescue!

32



### Herman Hollerith to the Rescue

- Herman Hollerith developed a machine (and concepts) that saved the U.S.
- The machine used electricity (a new idea for the time)
- Could automatically read cards and quickly, accurately tabulate results



### Inventing a Solution for Sorting

- Invented the idea to Bucket Sort on <u>each digit of a key</u>
- Use multiple passes starting with the 1's digit and move upwards



### Herman Hollerith

- His system was used for the 1890 Census
- And, it only took 9 months!
- Ever since, some form of tabulating machine has been used



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37



38



39



40

# Hollerith observed: Bucket Sort was stable i.e. items did not change relative positions He took advantage of this to sort data regardless of the size of the key

Radix Sort

- The *Radix Sort* was developed by *Herman Hollerith* in 1887 (77 BBW)
- The sort is completely noncomparative
- It uses a multiple Bucket Sort passes to sort data



### How it Works

- Radix Sort uses a Bucket Sort on each digit on the key
- This is done from the Least Significant Digit (LSD) to the most (MSD)
- After each pass, the buckets are the emptied into another set of buckets based on the <u>next</u> digit

43

### How it Works

- So, the number of buckets is equal to the number of <u>possible</u> digits
- Different "digits" can also be used:
  - base-10 digits for numbers (10 buckets)
  - or a single bit in the key (2 buckets)
  - or several binary bits as a group e.g. every 4 bits for  $2^4 = 16$  buckets























### Time Complexity of Radix Sort

- How many passes?
  - the algorithm will pass over the array equal to the total number of digits in the key  $({\bf k})$
  - e.g. for, a phone number, k = 10
- So...
  - we will exam n array elements a total k number of times
  - so, it will be O(k × n)

56

# Auxiliary Storage of Radix Sort How many buckets? we need auxiliary storage for each array element and for a bucket for each digit for a base-10 number, the number of buckets b = 10 So... we will need an extra n array elements and b buckets so, it will be O(b + n)

### 57

### Radix Summary

Time Average	$O(k \times n)$ where k is the # of key digits	
	O(K × II) WHELE K IS UIE # OF KEY UIGHS	
Time Best	$O(k \times n)$ actually a slow $O(n)$	
Time Worst	O(k × n) actually a slow O(n)	
Auxiliary space	O(b + n)	
Stable	Yes	
Online?	No	